電磁波

Fig. 1

- 1. An EM-wave with electric field intensity $\vec{E}_i = \hat{a}_i A e^{-\beta z}$ is traveling in free space as shown in Fig. 1.
- (a) What is the direction of propagation of the EM-wave? (2 points)
- (b) Find the magnetic field intensity \bar{H}_i (3 points) (c) What is k? (3 points)
 - (d) If the wave impinges on a perfect conducting plate placed
 - at z = 0, find the resultant electric field intensity \vec{E}_t and the resultant magnetic field intensity \vec{H}_i in medium 1.
- (10 points)
- (e) Find the electric and magnetic field intensity in medium 2
- 2. There are two waves $g_1(z,t)$ and $g_2(z,t)$. $g_1(z,t) = A\cos(\omega_1 t k_1 z)$, $g_2(z,t) = A\cos(\omega_2 t k_2 z)$.
 - If $\omega_1 = 1,000,001$, $\omega_2 = 999,999$, $k_1 = 1001 \times 10^{-2}$, $k_2 = 999 \times 10^{-2}$. (a) Find the resultant wave $f(z,t) = g_1(z,t) + g_2(z,t)$ (5 points) (b) Find the phase velocity v_p and the group velocity v_g of the resultant wave. (5 points)
- 3. A uniform plane wave with electric field intensity E in x-direction is traveling in z-direction in a
 - source-free and lossless free space with permittivity $\varepsilon_0 = (36\pi)^{-1} \times 10^{-9} F/m$ and permeability $\mu_0 (= 4\pi \times 10^{-7} H/m)$.
 - (a) Try to write the wave equation of the electric field intensity,
 - (b) How could Maxwell derive this wave equation from the Maxwell's equations? (10 points) (c) What is the speed of this wave in free space? (5 points)
- 4. Two IC are connected together with two sections of transmission lines. The voltage at the output of the driver IC is as shown in Fig. 2. Find the characteristic impedance (Z_{01} and Z_{02}) and time delays $(t_{d1} \text{ and } t_{d2})$ of both lines, and the unknown load R_L . (15 points)

(背面仍有題目,請繼續作答)

Fig. 2

- 5. A rectangular waveguide is to be designed to propagate the dominant TE10 mode and to exclude al other modes. The frequency of operation is to be 15 GHz and the guide is air-filled. Determine a set of guide dimensions such that 15 GHz is 25 percent above the TE₁₀ cutoff frequency and 25 percent below the cutoff frequency of the next higher-order mode. Calculate the wave impedance and wavelength along the direction of the waveguide for TE₁₀ mode at 15 GHz. (20 points)
- Given a characteristic impedance 50 Ω and a load impedance $Z_L = 100 j$ 50 Ω , match the line to the given load using only transmission line sections. (Hint: you may use the Smith chart below, temporarily. But don't forget to write down important procedures and results on your answer sheet Otherwise it will not be graded.) (15 points)

