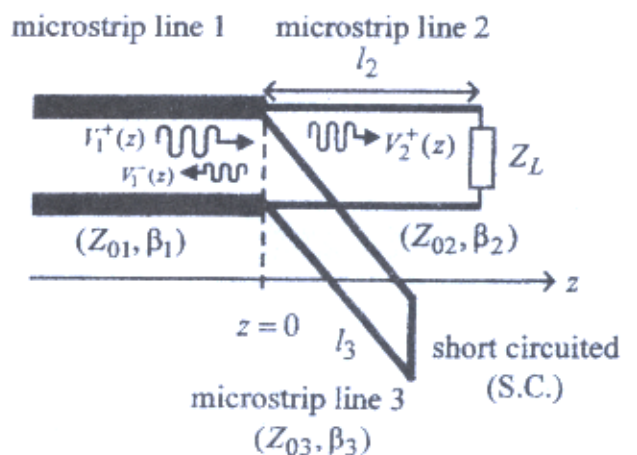
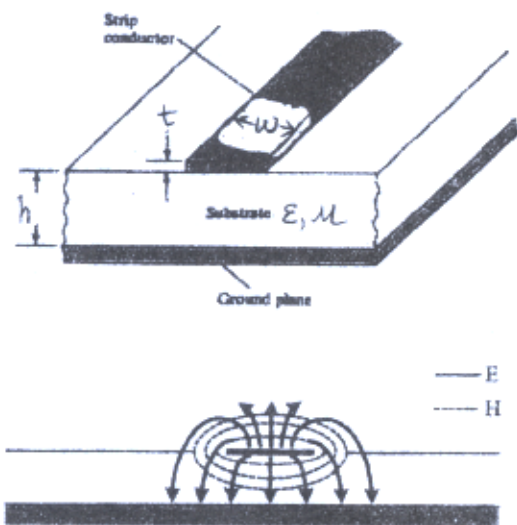


* Useful constants : $\epsilon_0 = 10^{-9}/(36\pi)$ (F/m); $\mu_0 = 4\pi \times 10^{-7}$ (H/m); $C = 3 \times 10^8$ (m/s)

1. (a) Write down the formula of the **displacement current density** and the generalized **Ampere's law** (with the **displacement current density**) in the Maxwell's equations. (5%)
 (b) Explain what is the difference between the **displacement current** and the **free current**? (5%)
2. Determine the **attenuation ratio (dB)** and the **phase velocity u_p** of a **plane wave** ($f = 100\text{MHz}$) at a distance of 100m below the surface of the sea water ($\epsilon_r = 80$, $\sigma = 5(\text{S/m}) @ f = 100\text{MHz}$). (10%)

Note that the complex propagation constant in a good conductor is $\gamma \approx \frac{(1+j)}{\sqrt{2}} \sqrt{\omega\mu_0\sigma}$

3. The illustration of the microstrip (transmission) line are shown in the following figures. The microstrip-line 1 ($Z_{01}=50\Omega$) is connected to a parallel connection (at $z = 0$) of the microstrip-line 2 ($Z_{02} = 100\Omega$, $l_2 = 0.25 \lambda$) with a load Z_L and the microstrip-line 3 ($Z_{03} = 100\Omega$, $l_3 = 0.25 \lambda$) with a short-circuited (S.C.) load. ($f = 1 \text{ GHz}$)
 (a) Explain why the microstrip line can not support a **pure TEM wave**. (5%)
 (b) Determine the line width (W) and length (l) of the microstrip line 2 (substrate $\epsilon_r = 4$ and $h = 1\text{mm}$). * Use the simple parallel-plate formula with TEM wave approximation. (10%)
 (c) If $Z_L = 250\Omega$ and the incident voltage (signal wave) is $V_1^+(z) = V_0 e^{-j\beta_1 z}$ in the microstrip line 1, determine the **reflection coefficient (Γ)** and the **SWR** at the point of $z = 0$ and write down the reflected voltage (wave), $V_1^-(z)$, in the microstrip line 1. (15%)
 (d) If the microstrip-line 1 is a lossless transmission line and the distributed parameter $L = 1.25 \text{ nH/m}$, determine the **distributed parameter C** (pF/m) and the **propagation constant β_1** at $f = 1\text{GHz}$. (10%)
 (β_1)



(背面仍有題目,請繼續作答)

4. Waveguide Problem

An **automotive tunnel** (汽車隧道) with a rectangular cross section (*width* $a = 15\text{m}$ & *height* $b = 6\text{m}$) is with **metal walls**. If we treat this tunnel as a **waveguide** :

- (a) Determine the **lowest frequency** of the radio wave that will propagate through this tunnel and write down the mode (TE_{mn} or TM_{mn}) of this wave. (5%)
- (d) Let the **length of the tunnel** is **100 m** and a **12-MHz radio wave** propagating into this tunnel (assuming the tunnel wall made of aluminum 鋁 $\sigma_c = 4 \times 10^8$). Find the **total attenuation** (dB) of this radio wave through this tunnel. (10%)
- (f) Determine the VSWR of the radio wave at the other side of the tunnel-waveguide (like having a free-space load). (5%)

Note: Waveguide wavelength & TE_{10} -mode impedance

$$\lambda_g = \lambda / \sqrt{1 - (f_c/f)^2} \quad \& \quad Z_{TE} = \eta_0 / \sqrt{1 - (f_c/f)^2}$$

Waveguide TE_{10} mode attenuation constant :

$$\alpha_{cTE10} = \frac{\lambda}{b\lambda_g} \sqrt{\frac{\pi}{\lambda\eta_0\sigma_c}} \left[1 + (\lambda_g/\lambda_c)^2 \left(1 + 2\frac{b}{a} \right) \right]$$

5. As shown in the following figure, let the **input power** P_i to a Hertzian dipole antenna (with a uniform current distribution I) is $P_i = 1\text{ W}$ and $f = 1\text{ GHz}$, $h = 10\text{ m}$.

- (a) What kind of polarization of the far-zone radiated wave from this Hertzian dipole. (5%)
- (b) Determine the **radiation power density** p_{av} (or S) (W/m^2) from the Hertzian dipole antenna at a cellular phone **handset** for a distance of $d = 100\text{ m}$. (15%)

*Note: The **current** of the Hertzian dipole antenna can be determined from the **antenna input power** P_i which is equal to the **radiation power** $P_{rad} = \eta_0(kI)^2/12\pi$

