編號:

216. 211, 226

國立成功大學九十七學年度碩士班招生考試試題

共/頁,第/頁

系所:微電子工程研究所、電机条、電通 所甲丁組

科目:工程數學

本試題是否可以使用計算機: □可使用 , □不可使用 (請命題老師勾選)

考試日期:0301,節次:3

- Find the curve y(x) that passes through (1, 0.5) and is such that at each point (x, y) the intercept of the tangent on the y-axis is equal to 2xy².
 (15%)
- 2. Solve the following initial value problems.

(a)
$$x^2y'' - 4xy' + 4y = 0$$
, $y(1) = 4$, $y'(1) = 13$. (10%)

(b)
$$(x^2D^2-5xD+8)y = 0$$
, $y(1) = 5$, $y'(1) = 18$. (10%)

3. Compute

$$\int_0^\infty \frac{\sin^2 x}{x^2} dx \qquad (15\%)$$

4. What is the order of the pole at z = 0 of the following function? Why?

$$f(z) = \frac{1}{(2\cos z - 2 + z^2)^2}$$
 (15%)

5. Find the Singular-Value Decomposition (SVD) of the matrix

$$A = \begin{bmatrix} 5 & 0 & 1 & 0 \\ 1 & 0 & 5 & 0 \\ 0 & 4 & 0 & -4 \end{bmatrix}. \tag{15\%}$$

6. Let
$$f(t) = e^{-|t|}$$
, and $g(t) = \begin{cases} 1, & -1 \le t < 1 \\ 0, & \text{otherwise} \end{cases}$ (20%)

- (a) Compute y(t) = f(t) * g(t), where * denotes convolution.
- (b) Find the Fourier transform of y(t).