編號:

207, 220

國立成功大學九十八學年度碩士班招生考試試題

共 / 頁,第/頁

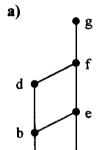
系所組別: 電機工程學系丁組,電腦與通信工程研究所甲組

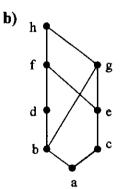
考試科目: 離散數學

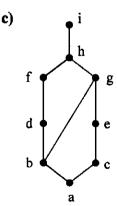
考試日期:0307, 節次:3

※ 考生請注意:本試題 ☑可 □不可 使用計算機

- 1. Let G be a loop-free undirected graph on $n \ (\ge 3)$ vertices. If G has only one vertex of even degree, how many vertices in \overline{G} have even degree? (15%)
- 2. Let k, m be fixed integers. Find all values for k, m for which (Z, \oplus, \odot) is a ring under the binary operations $x \oplus y = x + y k$, $x \odot y = x + y mxy$, where $x, y \in Z$. (15%)
- 3. In how many ways can the seven (identical) horses on a carousel be painted with black, brown and white paint in such a way that there are three black, two brown, and two white horses? (15%)
- 4. For $n \ge 1$, the *n*th triangular number t_n is defined by $t_n = 1 + 2 + ... + n = n(n+1)/2$. Find and solve a recurrence relation for s_n , $n \ge 1$, where $s_n = t_1 + t_1 + ... + t_n$, the sum of the first n triangular numbers. (15%)
- 5. Please derive a minimum state diagram of a *mealy*-style clocked sequential circuit with one input A and one output Z. When the circuit is turned ON, the output assumes the value of the first input signal. The output Z will then change vale only if three consecutive input signals have the same *opposite* value of output Z. (15%)
- 6. Determine whether the posets with following *Hasse* diagrams are lattices and give your reasons. (15%)







7. Find the generating function for the following sequence (For example, in the case of sequence 0, 1, 3, 9, 27, ..., the answer required is x/(1-3x), not $\sum_{i=0}^{\infty} 3^i x^{i+1}$ or simply $0+x+3x^2+9x^3+\ldots$): 0, 0, 1, a, a^2 , a^3 , ..., $a \neq 0$. (10%)