※ 考生請注意：本試題不可使用計算機。 請於答案卷（卡）作答，於本試題紙上作答者，不予計分。

1．（30\％）Consider a monopolized industry facing the inverse market de－ mand $P=630-2 Q$ ．The monopolist bears the total cost $c(Q)=Q^{2} / 2$ when producing $Q$ units．Suppose the government is considering to impose a tax on the transaction of the products．
（a．）（5\％）If the government charges a specific（quantity）tax so that con－ sumers pay an additional $\$ 30$ for every unit purchased，find the amount of tax the government can collect．
（b．）（5\％）Instead suppose the government uses the ad valorem（value）tax system so that consumers pay a fixed percentage $\tau$ of the price as the tax for every unit purchased．Find the tax rate $\tau$ the government should impose if it wants the market output level under $\tau$ to be the same as that in question （a）．
（c．）$(5 \%)$ Continue on（b），find the amount of tax the government can collect under that tax rate．
（d．）$(5 \%)$ If the monopolist acts as a competitive seller，find again the amount of tax the government can collect if it charges a specific tax of $\$ 30$ per unit．
（e．）（5\％）If the monopolist acts as a competitive seller，find again the tax rate $\tau$ the government should impose if it wants the market output level un－ der $\tau$ to be the same as that in question（d）．
（f．）$(5 \%)$ Continue on（e），find the amount of tax the government can collect under that tax rate．

2．$(20 \%)$ A monopolist is selling products to a competitive buyer with the inverse demand $P=120-2 Q$ ．The monopolist bears the total cost $c(Q)=Q^{2} / 2$ when producing $Q$ units．
（a．）（5\％）If the monopolist sells with the declining－block prices so that the buyer pays $P_{1}$ for each unit of the quantity under $Q_{1}$ units and $P_{2} \leq P_{1}$ for each additional unit over $Q_{1}$ ．Design the optimal $P_{1}, P_{2}$ and $Q_{1}$ for the monopolist．
（b．）$(5 \%)$ Find the amount of deadweight loss when the monopolist sells with the declining－block prices in question（a）．
（c．）$(5 \%)$ Suppose instead the monopolist uses a two－part tariff $T=A+B \cdot Q$ where $A$ is the lump－sum upfront payment，$B$ is the price the buyer pays for each additional unit and $T$ is the total amount of money the consumer pays in total when buying $Q$ units．Design the optimal $A$ and $B$ for the monopo－ list．
（d．） $5 \%$ ）Find the amount of deadweight loss if the monopolist sells with the two－part tariff in question（c）．
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3．（ $10 \%$ ）Suppose that $Q(p)$ is a linear demand function．We have known that，at price $\mathrm{p}=6$ ，the quantity demanded is 80 and the price elasticity of demand is -3 ．Find the demand function $Q(p)$ ．

4．$(10 \%)$ Let $Q(p)$ be a market demand function，where $p$ is price．The definition of revenue is $R=p Q(p)$ ．Is the following statement true？

## If the revenue $\boldsymbol{R}$ decreases as price $p$ increases， then the demand of the good is elastic．

Explain your answer by calculus．

5．$(10 \%)$ Let $u(x, y)=x+y$ and $v(x, y)=\sqrt{x}+\sqrt{y}$ be two utility functions．Do both utility functions represent the preferences in the same way？Explain your answer．

6．（20\％）A firm uses labor（ $L$ ）and capital（ $K$ ）to produce a single output．Its production function is given by $f(L, K)=(\sqrt{L}+\sqrt{K})^{2}$ ．Assume the prices of labor and capital are 2 and 3，respectively．
（a）（6\％）Find the firm＇s long－run total cost function．
（b）（ $8 \%$ ）Assume the capital is fixed at $K=16$ ．Find the solution to the firm＇s short－run cost minimization problem and find the firm＇s short－run total cost function．
（c）（6\％）Find the elasticity of substitution for $f(L, K)$ ．

