

1. Please briefly describe what is "calculus". (15%)
2. Who invented "calculus" in the 17<sup>th</sup> century? (10%)
3. PROOF. (15%)  
If  $f$  is the function defined by:  
$$f(x) = 2x + 1 \quad \text{for } x \leq 0$$
$$f(x) = x^2 - x \quad \text{for } x > 0$$
then  $\lim_{x \rightarrow 0} f(x)$  does not exist for  $x \rightarrow 0$ .
4. Differentiate  $f(x) = (\sec 4x + \tan 2x)^5$ . (10%)
5. Find the area between the curves: (15%)  
 $y = 4x$  and  $y = x^3$   
from  $x = -2$  to  $x = 2$ .
6. Evaluate  $\int (x^2 - 1)(x^3 - 3x + 2)^3 dx$  from  $x = 0$  to  $x = 2$ . (10%)
7. Calculate  $\int x \sin 2x dx$ . (10%)
8. PROOF. (15%)  
The length of the circumference of a circle with radius  $r$  is  $2\pi r$ .