

※ 考生請注意：本試題 可 不可 使用計算機

1. Write down the Stokes's theorem and explain why the Stokes's theorem sustains. (20%)
2. Derive the transformation matrix from Cartesian coordinate to cylindrical coordinate. Give a point $K(3, -4, 2)$ and Vector $\mathbf{B} = (x+y)\mathbf{i}_y + x\mathbf{i}_z$. Express K and \mathbf{B} in cylindrical coordinate and Evaluate \mathbf{B} at K in the Cartesian and cylindrical coordinates. (20%)
3. A transmission line with 400m length in the circuit is shown in Figure 1. Calculate the voltage at point a and point b at (1) $t=5\mu\text{s}$ and $t=7\mu\text{s}$. Wave velocity $u=2 \times 10^8$ m/s and the switch is closed at $t=0$. (20%)
4. For a magnetic vector potential $\mathbf{B} = -\rho^2 \mathbf{i}_z$ Wb/m, calculate the total magnetic flux crossing the surface $\phi = \pi/2$, $2\text{m} \leq \rho \leq 4\text{m}$, $0 \leq z \leq 2\text{m}$ (20%)
5. A coaxial cable with an insulating material of conductivity σ has the radius a of the central wire and the radius b of the whole cable. Show the resistance R of the cable per unit length, $R = [\ln(b/a)] / (2\pi\sigma)$. (20%)

