

1. Derive curl \mathbf{A} ($\nabla \times \mathbf{A}$) by using the line integral in the perpendicular coordinates (10%), express $\nabla \times \mathbf{A}$ in the cylindrical coordinates (10%), Explain the Stoke's theorem (10%).
2. Derive the capacitance of a coaxial cylinder (L, length; a, inner radius; b, outer radius), which is filled with a homogeneous dielectric with permittivity ϵ . Assume the inner and outer conductors carry $+Q$ and $-Q$, respectively. (20%)
3. A charged particle of mass 2kg and charge 4 Coulomb starts at point (1,1,0) with initial velocity $(3 \mathbf{a}_x + 4 \mathbf{a}_z \text{ m/s})$ in an electrical field $(6 \mathbf{a}_x + 5 \mathbf{a}_y \text{ V/m})$. At time $t=2$ second, determine (a) the acceleration of the particle, (b) its velocity, (c) its kinetic energy, (d) its position. (20%)
4. In free space, $\mathbf{E}=10\cos(\omega t-20x) \mathbf{a}_y \text{ V/m}$. Calculate (a) displacement current density \mathbf{J}_d , (b) magnetic field density \mathbf{H} . (10%)
5. In a lossless medium for which $\eta=40\pi$, $\mu_r=2$, and $\mathbf{H}=-0.2\cos(\omega t-z) \mathbf{a}_x + \sin(\omega t-z) \mathbf{a}_y \text{ A/m}$, calculate ϵ_r , ω , and \mathbf{E} . (20%) [$\eta=(\mu/\epsilon)^{0.5}$, $\beta=\omega(\mu\epsilon)^{0.5}$, $\epsilon_0=(1/36\pi) \times 10^{-9}$, $\mu_0=4\pi \times 10^{-7}$]