

本試題是否可以使用計算機： 可使用， 不可使用（請命題老師勾選）

1. (10 points) Evaluate the definite integral

$$\int_{-\pi}^{\pi} (\sin x + \cos x) dx.$$

2. (15 points) Find the formula for the integral

$$\int x e^x dx.$$

Hint: Use the formula for *integration by parts*,  $\int u dv = uv - \int v du$ .

3. (20 points) Determine the derivative  $f'(x)$ . In each case it is understood that  $x$  is restricted to those values for which the formula for  $f(x)$  is meaningful.

(a)

$$f(x) = x\sqrt{1+x^2}.$$

(b)

$$f(x) = \frac{1}{1+e^{-x}}.$$

4. (20 points) Ten students take a test. The scores are as follows:

116 91 130 120 114 99 118 102 119 113

Let  $x_1 = 116, x_2 = 91, \dots, x_{10} = 113$ . Find the expression for the quantity,  $\alpha$ , that minimizes the sum of squared deviations  $\sum_{i=1}^{10} (x_i - \alpha)^2$ .

(背面仍有題目,請繼續作答)

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科目：微積分

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5. (20 points) A hungry rat is placed in a T-maze. On one end of the maze, food can be obtained by a pressing bar. The rat runs the maze 10 times and the data are shown below:

0 0 1 1 1 0 1 1 1 1

The number 1 indicates that the rat gets the food and the number 0, otherwise. Suppose that, on each trial, the probability that the rat finds the food is  $\theta$ . The likelihood of the data is given by

$$(1 - \theta)^3 \theta^7$$

Find the value of  $\theta$  such that the likelihood of the data is maximized. (Hint: The maximum of a function, if it exists, is the same as the maximum of the logarithm of the function.)

6. (15 points) Compute  $\lim_{x \rightarrow 0} \frac{1 - e^{2x}}{x}$ .