

PART I:
ALGORITHM

- Let $X[1..n]$ and $Y[1..n]$ be integer arrays, each sorted in nondecreasing order. Write an $O(\log n)$ algorithm that finds the k_{th} smallest of the $2n$ combined elements, where $1 \leq k \leq n$.
- If k is a nonnegative constant then the solution of the recurrence

$$T(n) = \begin{cases} k, & n=1 \\ 3T(n/2)+kn, & n > 1 \end{cases}$$

for n a power of 2 is $T(n) = 3 * k * n^{\log_2 3} - 2 * k * n$.

Prove this statement.

- True or False (defend your answer): the following nondeterministic algorithm solves the No Partition Problem in nondeterministic polynomial time.

```

S:={};
p:=1;
while p≤n do
    q:=select({0,1})
    if q=1 then
        S:= SU{p}
    endif
    p:=p+1;
endwhile
if

```

$$\sum_{i \in S} c_i \neq \sum_{i \notin S} c_i$$

```

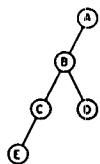
then
    success, print("yes")
else
    failure, print("no")
endif

```

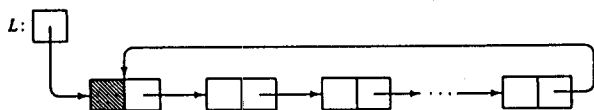
PART II

DATA STRUCTURE

1. Draw the internal memory representation of the following binary tree using (a) sequential, (b) linked, and (c) threaded linked representations. (15%)



2. Write a simple, nonrecursive algorithm to *reverse* a circular list of the type in the following figure. (12%)



3. If $X=(x_1, x_2, \dots, x_m)$ and $Y=(y_1, y_2, \dots, y_n)$ are strings where x_i and y_j are letters of the alphabet, then X is less than Y if $x_i = y_i$ for $1 \leq i < j$ and $x_j < y_j$ or if $x_i = y_i$ for $1 \leq i \leq m$ and $m < n$. Write an algorithm which takes two strings X, Y and returns either $-1, 0, +1$ if $X < Y, X = Y$ or $X > Y$ respectively. (12%)
4. In a given connected weighted graph G , suppose there exists an edge e_s whose weight is smaller than that of any other in G . Prove that every minimum cost spanning tree in G must contain e_s . (11%)