共2頁,第1頁

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科目:程式設計

本試題是否可以使用計算機: □可使用 , ☑不可使用 (請命題老師勾建)

Algorithms (50%)

- 1. (10%) Answer TRUE or FALSE for the following equation: $n^2 + n \lg n + \frac{1}{2}n = O(n^8)$
- 2. (15%) Solving the recurrence $T(n) = 2T(\sqrt{n}) + \lg n$ using big-O notation as tight as possible.
- 3. (10%) Consider the following two problems in which we are given a directed graph G=(V, E) and vertices $u, v \in V$.

Unweighted shortest path problem: Find a path from u to v consisting of the fewest edges.

Unweighted longest simple path problem: Find a path from u to v consisting of the most edges.

- (a) (5%) Determine which problem can be solved using the dynamic-programming in polynomial time.
- (b) (5%) Determine which problem cannot be solved using the dynamic-programming in polynomial time, and also give the reason.
- 4. (15%) Given a sequence $K = \langle k_1, k_2, \dots k_n \rangle$ of n distinct keys in sorted order such that $k_1 < k_2 < \dots < k_n$, and we wish to build a binary search tree from these keys. For each key k_i , we have a probability p_i that a search will be for k_i . Some searches may be for values not in K, and so we also have n+1 "dummy keys" $d_0, d_1, d_2, \dots, d_n$ representing values not in K. In particular, d_0 represents all values less than k_1, d_n represents all values greater than k_n , and for $i=1,2,\dots,n-1$, the dummy key d_i represents all values between k_i and k_{i+1} . For each dummy key d_i we have a probability q_i that a search will correspond to d_i . Each key k_i is an internal node, and each dummy key d_i is a leaf. Every search is either successful (finding some key k_i) or unsuccessful (finding some dummy key d_i), and so we have $\sum_{i=1}^{n} p_i + \sum_{i=0}^{n} q_i = 1$. The expected cost of a search tree T is

 $E[\text{search cost in } T] = \sum_{i=1}^{n} (depth_{T}(k_{i}) + 1) \cdot p_{i} + \sum_{i=0}^{n} (depth_{T}(d_{i}) + 1) \cdot q_{i} =$

 $1 + \sum_{i=1}^{n} depth_{T}(k_{i}) \cdot p_{i} + \sum_{i=0}^{n} depth_{T}(d_{i}) \cdot q_{i},$

where $depth_T$ denotes a node's depth in the tree T. Given five keys with $p_1 = 0.15$, $p_2 = p_4 = q_5 = q_1 = 0.10$, $p_3 = q_0 = q_2 = q_3 = q_4 = 0.05$, $p_5 = 0.20$, compute the corresponding smallest search cost.

圖立成功太學九十五學年度碩士班招生考試試題 共 2 頁,第2]

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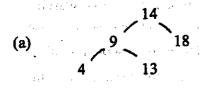
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5. (10%) True/False Question

- a. A complete binary tree is also an AVL tree
- b. Radix sort can only be performed on sequential lists, not on linked lists
- c. For a complete binary tree represented in memory as an array, if there is a node at index 4i+3 it must be a child of a child (grandchild) of the node at i.
- d. When applied to an already sorted list, quick sort shows its worst-case complexity. When applied to a reverse-sorted list, quick sort shows its best-case complexity.
- e. Searching for a key in a heap takes worst-case time O(n).
- 6. (15%) Given a binary search tree(BST), three traversals have been defined: preorder, inorder, and postorder. It returns the relative position of a node in the corresponding traversal. Given the following preorder traversal of a binary search tree

List the results of the other two traversals and draw the corresponding BST tree as well.

7. (10%) Assume that the trees below are AVL trees. First inset a new node with a key of 12 into (a). Next, insert a new node with a key of 3 into (b), For both parts, show the trees before and after each rotation you perform.



- 8. (15%) Given a string S, and we determine if the string S satisfies the following conditions
 - a. S contains repeated characters such as xxxyy form (x and y are characters)
 - b. S contains ABA' form, where A is a sub-string containing characters different from sub-string B, and A' is the reverse form of A.

Design the data structure and describe the procedure.