－Data Structures（ $50 \%$ ）
1．（ $30 \%$ ）
For the AOE（Activity on Edge）network described by the table，（a）what is the earliest time the project can finish？（15\％）（b）Please list all critical paths．Note that state 1 is the starting state and state 10 is the goal state．（ $15 \%$ ）

| Activity | From state | To state | Time |
| :--- | :--- | :--- | :--- |
| $a_{1}$ | 1 | 2 | 5 |
| $a_{2}$ | 1 | 3 | 5 |
| $a_{3}$ | 2 | 4 | 3 |
| $a_{4}$ | 3 | 4 | 6 |
| $a_{5}$ | 3 | 5 | 3 |
| $a_{6}$ | 4 | 6 | 4 |
| $a_{7}$ | 4 | 7 | 4 |
| $a_{8}$ | 4 | 5 | 3 |
| $a_{9}$ | 5 | 7 | 1 |
| $a_{10}$ | 5 | 8 | 4 |
| $a_{11}$ | 6 | 10 | 4 |
| $a_{12}$ | 7 | 9 | 5 |
| $a_{13}$ | 8 | 9 | 2 |
| $a_{14}$ | 9 | 10 | 2 |

2．（20\％）Given the postorder sequence and the inorder sequence of a binary character tree is ELGQPXRM and EGLMPQRX，（a）is the tree uniquely defined？（10\％）（b） Please draw an example binary tree satisfying the above two sequence．（ $10 \%$ ）

二，Algorithms（50\％）
3．（20\％）Solving the recurrence $T(n)=8 T(n / 2)+\Theta\left(n^{2}\right)$ using $\Theta$ notation．

4．（20\％）Show how to sort $n$ integers in the range 0 to $n^{3}-1$ in $O(n)$ time．

5．（10\％）The Fibonacci numbers are defined by recurrence

$$
\begin{aligned}
& F_{0}=0 \\
& F_{1}=1 \\
& F_{i}=F_{i-1}+F_{i-2} \text { for } i \geq 2
\end{aligned}
$$

Give an $O(n)$－time dynamic－programming algorithm to compute the $n$th Fibonacci number．

