210

编號:

Probability and Statistics 2012 (100%)

- A producer of a certain type of electronic component ships to suppliers in lots of twenty. Suppose that 70% of all such lots contain no defective components, 20% contain one defective component, and 10% contain two defective components. A lot is selected and two components from the lot are randomly selected and tested and neither is defective.
- 1.1 Let A be the event that two components are selected from the lot, N be the event that a lot contains no defective component, O be the event that a lot contains one defective component, T be the event that a lot contains two defective components. Please find P(A|N), P(A|O) and P(A|T). [15%]

1.2 Using answers in **1.1**, what is the probability that one defective component exists in the lot? [5%] (Please write your answers in fraction with integer numerator and integer denominator.)

2. Consider the joint density function

f(x, y) =
$$\begin{cases} \frac{16y}{x^3}, & x > 2, & 0 < y < 1, \\ 0, & elsewhere. \end{cases}$$

2.1 Calculate the mean of its marginal distributions g(x) and h(y). [10%]

2.2 Calculate E(XY) and covariance σ_{XY} . [10%]

- **3.** Assuming that a Bernoulli trial can result in a success with probability p and a failure with probability q = l p. If a random variable X represents the number of successes in *n* independent trials.
- **3.1** What is the probability distribution of X? Please specify the name and mathematical form of this probability distribution. [10%]
- **3.2** Please derive mean and variance of the probability distribution in **3.1** using expectation operator. [10%]
- 4. If 10% of the residents in a U.S. city prefer a white telephone over any other color available.
- **4.1** Please find out the probability that among the next 5 telephones installed in that city, 1 is found to be white. [5%]
- **4.2** Please find out the probability that among the next 10000 telephones installed in that city, between 900 and 989 inclusive will be white (hint: use the included table to find your answer). [10%]
- **4.3** Please explain and examine that in **4.2**, which probability distribution you used and whether such approximation is applicable. [5%]

(背面仍有題目,請繼續作答)

- **5.** A random sample of 100 records in the United States during the past year showed an average life span of 72 years. Assuming a population standard deviation of life span is 8 years and we are interested to know whether this indicates that the mean life span today is greater than 70 years.
- 5.1 What are our null and alternative hypotheses? [10%]
- **5.2** Please examine whether our data indicate that the average life span in the United States is greater than 70 years when the level of significance is 0.05? [10%]

編號: 210

國立成功大學一〇一學年度碩士班招生考試試題

共 3 頁,第3頁

考試日期:0226・節次:3

系所組別: 醫學資訊研究所

考試科目: 機率統計

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