編號: 232 國立成功大學九十七學年度碩士班招生考試試題

共 / 頁,第/頁

系所: 醫學資訊研究所

科目:機率統計

本試題是否可以使用計算機: ☑可使用 , □不可使用

(請命題老師勾選)

考試日期:0301,節次:3

Probability & Statistics 2008 (100%)

[20%] Let X denote the number of times a certain numerical control machine will 1. malfunction: 1, 2, or 3 times on any given day. Let Y denote the number of times a technician is called on an emergency call. Their joint probability distribution is given as:

f(x, y)	x	1	2	3
	1	0.05	0.05	0.1
y	2	0.05	0.1	0.35
	3	0	0.2	0.1

- (a) Evaluate the marginal distribution of X.
- (b) Evaluate the marginal distribution of Y.
- (c) Find P(Y = 3 | X = 2).
- (d) Find the covariance of X and Y.
- [15%] At "busy time" a telephone exchange is very near capacity, so callers have difficulty placing their calls. It may be of interest to know the number of attempts necessary in order to gain a connection. Suppose that let p = 0.05 be the probability of a connection during busy time. What is the probability that 5 attempts are necessary for a successful call?
- [20%] Prove that the mean and variance of the gamma distribution with the following density function are $\mu = \alpha \beta$; $\sigma^2 = \alpha \beta^2$.

$$f(x) = \begin{cases} \frac{1}{\beta^{\alpha} \Gamma(\alpha)} x^{\alpha - 1} e^{-x/\beta}, & x > 0 \\ 0, & \text{elsewhere} \end{cases}$$

where $\alpha > 0$ and $\beta > 0$.

- [10%] A foreign student club lists as its members 2 Canadians, 3 Japanese, 5 Italians, and 2 4. Germans. If a committee of 4 is selected at random, find the probability that.
 - (a) all nationalities are represented;
 - (b) all nationalities except the Italians are represented.
- 5. [10%] Please describe Central Limit Theorem.
- [15%] A random sample of 100 recorded deaths in the United States during the past year 6. showed an average life span of 71.8 years. Assuming a population standard deviation of 8.9 years, does this seem to indicate that the mean life span today is greater than 70 years? Use a 0.05 level of significance.

This table indicates the area under the standard normal curve corresponding to P(Z < z)

z	.00	.01	.02	.03	.04	.05	
1.6	0.9452	0.9463	0.9474	0.9484	0.9495	0.9505	
1.7	0.9554	0.9564	0.9573	0.9582	0.9591	0.9599	
1.8	0.9641	0.9649	0.9656	0.9664	0.9671	0.9678	

[10%] Please draw normal curves with two cases: $\mu_1 = \mu_2$, $\sigma_1 < \sigma_2$; and $\mu_1 < \mu_2$, $\sigma_1 < \sigma_2$.