説明: 1.請依序作答並標明題號。 2. R = 8.314 J mol⁻¹K⁻¹

- 1. The reaction $A + B \rightarrow C$ takes place in two steps by the mechanism 2 A = D followed by $B + D \rightarrow A + C$ with rate constant k_2 . The first step comes to a rapid equilibrium with equilibrium constant K_1 . Derive an expression for the rate of formation of C in terms of K_1 , k_2 , [A], and [B]. (6%)
- 2. It is often said that near room temperature, a chemical reaction rate doubles with every 10° rise in temperature. Calculate the activation energy of a reaction at 300 °K that obeys this rule exactly. (6%)
- 3. Please explain the following photophysical processes in a photochemical reaction.

a. resonance fluorescence (2%)

b. intersystem crossing (ISC) (2%)

c. internal conversion (IC) (2%)

- 4. It is known that entropy changed is greater than zero (dS > 0) for a spontaneous reaction. Based on this, please show that dG (Gibbs free energy) < 0 is required for a spontaneous reaction. (8%)
- 5. An ideal gas absorbs 9410 J of heat when it is expanded isothermally (at 25 °C) and reversibly from 1.5 dm³ to 10 dm³. How many moles of the gas are present? (6%)
- 6. The constant-pressure heat capacities of gaseous hydrogen, oxygen, and water are 29.0, 29.5, and 33.6 J mole⁻¹K⁻¹, respectively. Assume that heat capacities are independent of temperature. The enthalpy of formation of gaseous water at 25 °C is 241.82 KJ mol⁻¹. What is its value at 100 °C? (8%)
- 7. If the ionization constant of a molecule could be described by the equation

 $\ln K = 7 - 1850/T - 0.002T$

between 5 °C and 55 °C. Calculate values of ΔG° and ΔH° for the ionization at 50 °C. (10%)

- 8. Evaluate the following commutators:
 - (a) $\left[\frac{d}{dx}, x^2 \right]$

(4%)

- (b) $[\hat{x}, \hat{p}_x], \hat{x}$: operator corresponding to the x coordinate, \hat{p}_x : operator for the x component of linear momentum. (4%)
- 9. If ψ_1 , ψ_2 , and ψ_3 are wave functions with a degenerate energy E, please show that any linear combination $c_1\psi_1 + c_2\psi_2 + c_3\psi_3$ is still a wave function. (8%)
- 10. (a) Find the term symbols, ^{2S+1}L_J, resulting from non-equivalent electrons, pp. (6%)
 - (b) Please determine the ground-state term symbol for d^6 electronic configuration. (4%)
- 11. (a) Please write the complete Hamiltonian operator for hydrogen molecule (H₂). (3%)
 - (b) What is Born-Oppenheimer approximation? (3%)
 - (c) If Born-Oppenheimer is applied, then how to construct molecular Hamiltonian operator for H_2 . (3%)
- 12. Find the normalization constant for the molecular orbital $c(1S_A + 1S_B)$ in terms of the overlap integral S, where c is normalization constant. (6%)
- 13. (a) Could we observe pure rotational spectrum for O₂ molecule? why? (3%)
 - (b) For CO₂, please specify the vibrational mode(s) with infrared active and explain your reason. (6%)