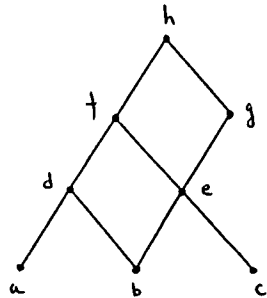
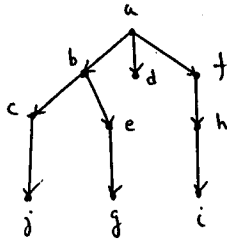


Part II:

1. Show that among $n+1$ arbitrarily chosen integers, there are two whose difference is divisible by n . 10 points
2. For a lattice L , show that a) implies b) in the following:
 - a) $a \vee (b \wedge c) = (a \vee b) \wedge (a \vee c)$ for all a, b, c in L .
 - b) $a \wedge (b \vee c) = (a \wedge b) \vee (a \wedge c)$ for all a, b, c in L .
 10 points
3. Consider the Hasse diagram of the poset R on $A = \{a, b, c, d, e, f, g, h\}$ on the right: Find
 - 1) upper bounds of $\{e, c\}$
 - 2) minimal elements
 - 3) least element
 - 4) greatest lower bound of $\{f, d\}$
 - 5) lower bounds of $\{h, f\}$
 15 points



4. Consider the labeled tree T whose digraph is shown below:



Draw the digraph of the corresponding binary positional tree $B(T)$. Label the vertices of $B(T)$ to show their correspondence to vertices of T . Suppose that visiting a node results in printing out the label of that node. Show the result of performing 1) preorder 2) inorder 3) postorder for $B(T)$. 20 points

5. Let $S = \{1, 2, 3, 4, 5\}$ and let $A = S \times S$. Define the following relation R on A : $(a, b) R (a', b')$ if and only if $ab' = a'b$.
 - 1) Show that R is an equivalence relation.
 - 2) Compute A/R .
 20 points