系所組別：太空與電㢡科學研究所

## 考試科目：電磁學

※ 考生請注意：本試題不可使用計算機
（1）Three hydrogen ions $\left(\mathrm{H}^{+}\right) \mathrm{A}, \mathrm{B}, \mathrm{C}$ are placed in the middle of a parallel－plate electric field with a potential difference of 10 volts， and a speedometer is installed in the edge of the electric field as shown in Figure 1．The initial kinetic energies $E_{k}$ and moving directions of these ions are also noted in the figure respectively． Please list these ions from high to low according their arrival velocities recorded by the speedometer，and give a brief explanation．（10\％）


Figure 1
（2）As shown in Figure 2，the electric field in the air at point $P$ on the surface of a cylindrical dielectric rod is $\sqrt{3} \hat{x}+5 \hat{y}$ ．Find the electric field inside the dielectric rod at point $P$ ．（10\％）


Figure 2
（3）A uniform line charge $\lambda$ is placed on an infinite straight wire，a distance $d$ above a grounded conducting plane．
（a）Find the potential $V$ in the region above the plane．（ $\mathbf{1 0 \%}$ ）
（b）Find the force on the wire per unit length．（ $\mathbf{1 0 \%}$ ）
（c）Find the surface charge density $\sigma$ induced on the conducting plane．（ $\mathbf{1 0 \%}$ ）
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（4）A cone of height $H$ and radius of base $R$ is permanently magnetized with uniform magnetization $M$ ．The vector $\vec{M}$ is collinear with the axis of the cone（see Figure 3）．Let that axis be $z$ ，and the apex of the cone the coordinate origin．What is the magnetic field along the $z$ axis， at the distance $h$ from the apex， $\bar{B}(h)$ ？（20\％）Here $h+z$ is larger than the thickness of the cone at the distance $z$ from its apex．
［Hint：model the cone as a stack of infinitesimal disks．］


Figure 3
（5）A rectangular frame of length $2 b$ along the $x$ axis and $a$ along the $y$ axis is moving with constant velocity $\vec{v}=v \hat{x}$ from $x=-\infty$ into the magnetic field $\vec{B}=\hat{z} B_{0} e^{\alpha x}$ ．The frame is made of wire with the resistance per unit length，$\rho$ ．
（a）If the center of the frame is at the position $x=x_{c}$ ，what is the flux through the frame？Show that the flux is proportional to $\sinh (\alpha b) .(7 \%)$
（b）When the center of the frame is at $x_{c}$ ，what is the electromotive force which is being generated in the frame as it is moving？（7\％）
（c）What is the power dissipated in the frame，as a function of $x_{c}$ ？（8\％）
（d）What is the total amount of heat generated by the current in the frame as it travels from

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x_{c}=-\infty \text { to } x_{c}=0 ?(\mathbf{8 \%})
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